

Transition to (spatio-temporal complexity and) turbulence in thermoconvection & aerodynamics

<http://emmanuelplaut.perso.univ-lorraine.fr/t2t>

Session	Date	Content
1 -	29/09	Thermoconvection: phenomena, equations, differentially heated cavity, cavity heated from below = RB cavity, linear stability analysis
2 -	06/10	RB Thermoconvection: linear stability analysis
3 -	13/10	RB Thermoconvection: (weakly) nonlinear phenomena
→ 4 -	20/10	Aerodynamics of OSF : linear stability analysis
5 -	27/10	Aerodynamics of OSF : linear & weakly nonlinear stability analyses
6 -	10/11	Aerodynamics of OSF : nonlinear phenomena
	24/11	Examination

RB* = Rayleigh-Bénard

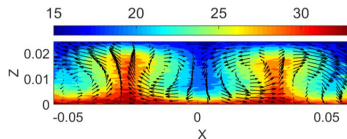
OSF* = Open Shear Flows

Today: session 4: transition in open shear flows:

- Introduction: OSF, instabilities of OSF, Rayleigh criterion
- Numerical linear stability analysis of plane Poiseuille flow: towards TS waves

Introduction: open shear flows, a new family of systems, quite different from Rayleigh-Bénard thermoconvection systems

RB Thermoconvection



[Leclerc & Métivier]

Fields

\mathbf{v}

T

Base state

$\mathbf{v} = \mathbf{0}$ trivial

$T = T(z)$

Eqs and nonlinearities

Navier-Stokes contains $(\mathbf{v} \cdot \nabla)\mathbf{v}$

Heat equation contains $\mathbf{v} \cdot \nabla T$

Open shear flows (OSF)



[Homsy et al.]

\mathbf{v}

$T = \text{constant}$

$\mathbf{v} \neq \mathbf{0}$ complex

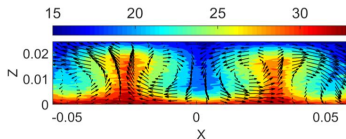
$T = \text{constant}$

Navier-Stokes contains $(\mathbf{v} \cdot \nabla)\mathbf{v}$

Heat equation trivially fulfilled

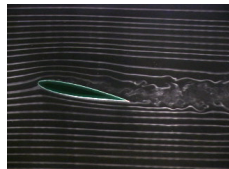
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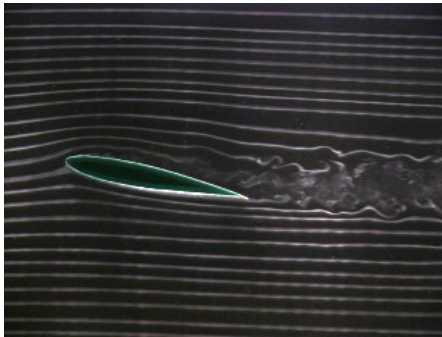
Heat equation trivially fulfilled

OSF quite interesting but also quite challenging:

easier to understand $\mathbf{v} \cdot \nabla T$ than $(\mathbf{v} \cdot \nabla)\mathbf{v}$!

Open shear flows are often encountered in aerodynamics

Turbulent (?) **flow** around an obstacle, an airfoil, at an angle of attack $\alpha = 15^\circ$, observed with smoke in a wind tunnel at U. Stanford:



[[Homsy et al. 2019 *Multimedia Fluid Mechanics Online*. Cambridge University Press](#)]

Open shear flows are often encountered in aerodynamics

Laminar flow around an obstacle, an airfoil, also exists, and may be computed, for the external flow, with potential flow theory - complex analysis techniques:

[[Plaut 2018 *Mécanique des fluides : des bases à la turbulence*. Cours Mines Nancy 2A](#)]

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When and how **laminar open shear flows** get **unstable** and go to **turbulence** ?